

AP Calculus AB Prerequisite Assignment

The purpose of this assignment is to have you practice the mathematical skills necessary to be successful in Calculus AB. All of the skills covered in this packet are skills from Algebra 2 and Pre-Calculus. If you need to, you may use reference materials to assist you and refresh your memory (old notes, textbooks, online resources, etc.). While the graphing calculators will be used in class, there are *no calculators allowed* on this packet. You should be able to do everything without a calculator.

AP Calculus AB is a fast paced course that is taught at the college level. There is a lot of material in the curriculum that must be covered before the AP exam in May. Therefore, we cannot spend a lot of class time re-teaching prerequisite skills. This is why you have this packet. Spend some time with it and make sure you are clear on everything covered in the packet so that you will be successful in Calculus. Of course, you are always encouraged to seek help from your teacher if necessary.

This assignment is for your practice only! It will not be graded or turned in. Just use it as needed to keep up your skills over the summer and prepare for a great AP Calculus course in the fall!

Good Luck!

Show all work!
No calculators!

Section I: Algebra Review

Identify the following statements as true or false.

1. $\frac{x+y}{2} = \frac{x}{2} + \frac{y}{2}$ _____

2. $\frac{1}{p+q} = \frac{1}{p} + \frac{1}{q}$ _____

3. $\frac{2k}{2x+h} = \frac{k}{x+h}$ _____

4. $3 \cdot \frac{a}{b} = \frac{3a}{b}$ _____

5. $3 \cdot \frac{a+b}{c} = \frac{3a+b}{c}$ _____

6. $\sqrt{a^2 + b^2} = a + b$ _____

Identify the following statements as true or false over the set of real numbers. Give a counter example for any false statement.

7. $x^3 + 1 > x^3$ _____

8. $x^3 + x > x^3$ _____

9. $x^2 \geq 0$ _____

10. $x^2 \geq x$ _____

11. $2x \geq x$ _____

12. $\sqrt{x} \geq 0$ _____

13. $-x \leq 0$ _____

14. $\frac{1}{x} \leq x$ _____

15. $x \leq |x|$ _____

16. Solve $xy' + y + 1 = y'$ for y' .

17. Solve $\ln y = kt$ for y .

16. _____

18. Factor: $y^3 + 27$

19. Factor: $x^2(x-1) - 4(x-1)$

17. _____

18. _____

19. _____

Simplify each expression.

20. $\frac{(x^2)^3 x}{x^7}$ _____

21. $\sqrt{x} \cdot \sqrt[3]{x} \cdot x^{\frac{1}{6}}$ _____

22. $\frac{5(x+h)^3 - 5x^3}{h}$ _____

23. $\frac{3(x+h)^2 - 3x^2}{h}$ _____

$$24. \frac{\frac{x^2-1}{x}}{\frac{x+1}{x^3}} \underline{\hspace{2cm}}$$

$$25. \frac{\frac{1}{x} + \frac{4}{x^2}}{3 - \frac{1}{x}} \underline{\hspace{2cm}}$$

$$26. \frac{\frac{a}{2x+h} - \frac{a}{2x}}{h} \underline{\hspace{2cm}}$$

$$27. \frac{1}{1-2a} - \frac{2}{1+2a} + \frac{6a+2}{4a^2-1} \underline{\hspace{2cm}}$$

Simplify, using factoring of binomial expressions. Leave answers in factored form.

Example:

$$\begin{aligned} \frac{(x+1)^3(4x-9)}{(x-6)(x+1)} &= \frac{(x+1)^2[(x+1)(4x-9) - (16x+9)]}{(x-6)(x+1)} \\ &= \frac{(x+1)^2(4x^2 - 5x - 9 - 16x - 9)}{(x-6)(x+1)} \\ &= \frac{(x+1)^2(4x^2 - 21x - 18)}{(x-6)(x+1)} \\ &= \frac{(x+1)^2(4x+3)(x-6)}{(x-6)(x+1)} \\ &= (x+1)(4x+3) \end{aligned}$$

$$28. (x-1)^3(2x-3) - (2x+12)(x-1)^2 \underline{\hspace{2cm}}$$

$$29. \frac{(x-1)^2(3x-1) - 2(x-1) \cdot 3}{(x-1)^4} \underline{\hspace{2cm}}$$

$$30. \frac{(x-1)^3(2x-3) - (4x-1)(x-1)^2}{(x-1)^2(2x-1)} \underline{\hspace{2cm}}$$

Simplify by rationalizing the numerator.

Example:

$$\frac{\sqrt{x+4}-2}{x} = \frac{\sqrt{x+4}-2}{x} \cdot \frac{\sqrt{x+4}+2}{\sqrt{x+4}+2} = \frac{x+4-4}{x(\sqrt{x+4}+2)} = \frac{x}{x(\sqrt{x+4}+2)} = \frac{1}{\sqrt{x+4}+2}$$

31. $\frac{\sqrt{x+9}-3}{x}$ _____

32. $\frac{\sqrt{x+h}-\sqrt{x}}{h}$ _____

Solve each equation or inequality for x over the set of real numbers.

33. $2x^4 + 3x^3 - 2x^2 = 0$ _____ 34. $\frac{2x-7}{x+1} = \frac{2x}{x+4}$ _____

35. $\frac{3x+5}{(x-1)(x^4+7)} = 0$ _____ 36. $\sqrt{x^2-9} = x-1$ _____

37. $|2x-3| = 14$ _____ 38. $x^2 - 2x - 8 < 0$ _____

Solve each of the systems.

39. $x + y = 8$ _____
 $2x - y = 7$ _____

40. $y = x^2 - 3x$ _____
 $y = 2x - 6$ _____

Section II: Pre-Calculus Review

Evaluate each of the following. Leave your answers in radical form.

41. $\sin(30^\circ)$ _____

42. $\cos\frac{2\pi}{3}$ _____

43. $\tan 45^\circ$ _____

44. $\sin\left(-\frac{\pi}{6}\right)$ _____

45. $\tan \pi$ _____

46. $\csc\frac{5\pi}{6}$ _____

47. $\cos(90^\circ)$ _____

48. $\cos\frac{3\pi}{4}$ _____

49. $\tan\frac{\pi}{6}$ _____

50. $\cos^{-1}\left(\frac{1}{2}\right)$ _____

51. $\sin^{-1}\left(\frac{\sqrt{2}}{2}\right)$ _____

52. $\tan^{-1}(1)$ _____

Solve each trigonometric equation for $0 \leq x \leq 2\pi$.

53. $\sin x = \frac{\sqrt{3}}{2}$ _____

54. $\tan^2 x = 1$ _____

55. $\cos\frac{x}{2} = \frac{\sqrt{2}}{2}$ _____

56. $2\sin^2 x + \sin x - 1 = 0$ _____

For each trigonometric function identify the amplitude and any horizontal or vertical shifts from the basic function.

57. $y = \frac{1}{2}\cos\frac{x}{2} - 3$ amplitude: _____ period: _____ vertical shift: _____

58. $y = 2\sin(2x - \pi)$ amplitude: _____ period: _____ horizontal shift: _____

59. $y = \tan 3x$ period: _____

Solve each exponential or logarithmic equation.

60. $5^x = 125$ _____

61. $8^{x+1} = 16^x$ _____

62. $81^{\frac{3}{4}} = x$ _____

63. $8^{\frac{-2}{3}} = x$ _____

64. $\log_2 32 = x$ _____

65. $\log_x \frac{1}{9} = -2$ _____

66. $\log_4 x = 3$ _____

67. $\log_3(x+7) = \log_3(2x-1)$ _____

Expand each of the following using the laws of logs.

68. $\log_3 5x^2$ _____

69. $\ln \frac{5x}{y^2}$ _____

Complete each of the following using trigonometric identities and formulas.

70. $\sin\left(\frac{\pi}{2} - x\right) =$ _____

71. $\sin^2 x + \cos^2 x =$ _____

72. $\sin 2u =$ _____

73. $\tan x =$ _____

74. $1 + \cot^2 x =$ _____

75. $1 - \cos^2 x =$ _____

76. A right triangle has a base of 5 and a hypotenuse of 7. Find the height.

Section III: Graphing Review

Sketch the following functions. State the domain and range of each. Draw and label your own axes.

77. $f(x) = x$

78. $f(x) = x^2$

79. $f(x) = x^3$

80. $f(x) = |x|$

$$81. f(x) = [x]$$

$$82. f(x) = \frac{1}{x}$$

$$83. f(x) = \sqrt{x}$$

$$84. f(x) = e^x$$

$$85. f(x) = \ln x$$

$$86. f(x) = \sqrt{9 - x^2}$$

$$87. f(x) = \sin x$$

$$88. f(x) = \cos x$$

$$89. f(x) = \tan x$$

$$90. f(x) = \csc x$$

$$91. f(x) = \sec x$$

$$92. f(x) = \cot x$$