

Today's Agenda:

- 1) Warm Up  
-review for quiz
- 2) Questions on Warm Up, HW, etc...
- 3) QUIZ on Composition
- 4) Use notes on inverses to try homework

**You can use a calculator on the quiz**

$$\text{Let } f(x) = x^{1/2} + 2, \quad g(x) = 3x^{1/2} - 1, \quad \text{and } h(x) = -2x^{1/2} + 3$$

1) Perform  $f(x) - g(x)$

$$-2x^{1/2} + 3$$

2) Perform  $g(x) - h(x)$

$$5x^{1/2} - 4$$

$$\text{Let } f(x) = 4x^{3/2}, \quad g(x) = 2x^{1/3}, \quad \text{and } h(x) = -6x^{1/2}$$

3) Perform  $f(x) \cdot h(x)$

$$-24x^2$$

4) Perform  $\frac{f(x)}{g(x)}$

$$2x^{7/6}$$

$$\text{Let } f(x) = 2x^{-1}, \quad g(x) = 2x + 5, \quad \text{and } h(x) = \frac{x - 4}{2}$$

5) Perform  $g(h(x))$

$$x + 1$$

6) Perform  $g(g(x))$

$$4x + 15$$

$$\text{Let } f(x) = 2x + 2, \quad g(x) = x^2, \quad \text{and } h(x) = \frac{3}{x - 2}$$

7) Perform  $\frac{f(x)}{g(x)}$

$$\frac{2(x + 1)}{x^2}$$

Domain:  $(-\infty, 0) \cup (0, \infty)$

8) Perform  $g(f(x))$

$$4x^2 + 8x + 4$$

Domain:  $(-\infty, \infty)$

NOTES: Inverse Function (Part 1)

Day 19

**To find the inverse function...**

From a Table:

**Switch** x and y values

From a Graph:

**Switch** x and y values of points

From an Equation:

1. Write the original function, using **y** to stand for  $f(x)$ .
2. **Switch** x and y.
3. Solve for y using inverse operations
4. Replace y with  **$f^{-1}(x)$** .

From a Table:

**Switch** x and y values

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**EXAMPLE 1:**

Table for  $f(x)$ :

$x$	-2	-1	0	1	2
$y$	4	2	0	-2	-4

Table for  $f^{-1}(x)$ :

$x$	<b>4</b>	<b>2</b>	<b>0</b>	<b>-2</b>	<b>-4</b>
$y$	<b>-2</b>	<b>-1</b>	<b>0</b>	<b>1</b>	<b>2</b>

Is the inverse a function?

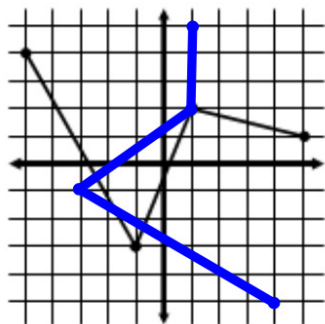
**Yes, there is exactly one output(y) for every input(x)**

From a Graph:

**Switch** x and y values of points

$f(x):$	$f^{-1}(x):$
$(-5, 4)$	$(4, -5)$
$(-1, -3)$	$(-3, -1)$
$(2, 1)$	$(1, 2)$
$(5, 1)$	$(1, 5)$

EXAMPLE 2:



Is the inverse a function?

**No, it fails the vertical line test**

From an Equation:

1. Write the original function, using y to stand for  $f(x)$ .
2. **Switch**  $x$  and  $y$ .
3. Solve for  $y$  using inverse operations
4. Replace  $y$  with  $f^{-1}(x)$ .

EXAMPLE 3:

$$y = \frac{1}{2}x + 5$$

$$x = \frac{1}{2}y + 5$$

$$\begin{array}{cc} -5 & -5 \end{array}$$

$$(2)(x - 5) = (1/2y)(2)$$

$$2x - 10 = y$$

$$\underline{\underline{f^{-1}(x) = 2x - 10}}$$

EXAMPLE 4:

$$y = (x - 4)^2 + 7$$

$$f(x) = (x - 4)^2 + 7$$

$$x = (y - 4)^2 + 7$$

$$\begin{array}{cc} -7 & -7 \end{array}$$

$$\sqrt{x - 7} = \sqrt{(y - 4)^2}$$

$$\sqrt{x - 7} = y - 4$$

$$\begin{array}{cc} +4 & +4 \end{array}$$
$$\sqrt{x - 7} + 4 = y$$

$$\underline{\underline{f^{-1}(x) = \sqrt{x - 7} + 4}}$$

**NOTATION:** If we have a function  $f(x)$ , the inverse will be named :  $f^{-1}(x)$

How do you find the inverse of a function?

**switch x and y**

Switching the x and y values means you are also switching the

**input** and **output**

**domain** and **range**