**Course Narrative**

**Course Title**: AP Calculus AB

**Course Description**: The purpose of the course is to develop mathematical thinking and a thorough understanding of the concepts and connections among concepts in calculus. The two major themes are the derivative as a rate of change and the integral as an accumulation function. Technology is used throughout the course and students are taught how to use graphing calculators to help solve problems, experiment, interpret results, and support conclusions.

**Learning expectations**:

The student will:

**Limits of functions**

• An intuitive understanding of the limiting process

• Calculating limits using algebra

• Estimating limits from graphs or tables of data

**Asymptotic and unbounded behavior**

• Understanding asymptotes in terms of graphical behavior

• Describing asymptotic behavior in terms of limits involving infinity

• Comparing relative magnitudes of functions and their rates of change

**Continuity as a property of functions**

• An intuitive understanding of continuity

• Understanding continuity in terms of limits  
• Geometric understanding of graphs of continuous functions (Intermediate Value Theorem and Extreme Value Theorem)  
  
**Concept of the derivative**• Derivative presented graphically, numerically and analytically  
• Derivative interpreted as an instantaneous rate of change  
• Derivative defined as the limit of the difference quotient  
• Relationship between differentiability and continuity  
  
**Derivative at a point**• Slope of a curve at a point. Examples are emphasized, including points at which there are vertical tangents and points at which there are no tangents  
• Tangent line to a curve at a point and local linear approximation  
• Instantaneous rate of change as the limit of average rate of change  
• Approximate rate of change from graphs and tables of values  
  
**Derivative as a function**• Corresponding characteristics of graphs of *ƒ* and *ƒ*’  
• Relationship between the increasing and decreasing behavior of *ƒ* and the sign of *ƒ*’  
• The Mean Value Theorem and its geometric interpretation  
• Equations involving derivatives  
  
**Second derivatives**• Corresponding characteristics of the graphs of *ƒ*, *ƒ*’ and *ƒ”*• Relationship between the concavity of *ƒ* and the sign of *ƒ”*• Points of inflection as places where concavity changes  
  
**Applications of derivatives**• Analysis of curves, including the notions of monotonicity and concavity  
• Optimization, both absolute (global) and relative (local) extrema  
• Modeling rates of change, including related rates problems  
• Use of implicit differentiation to find the derivative of an inverse function  
• Interpretation of the derivative as a rate of change in varied applied contexts, including velocity, speed and acceleration  
• Geometric interpretation of differential equations via slope fields and the relationship between slope fields and solution curves for differential equations  
  
**Computation of derivatives**• Knowledge of derivatives of basic functions, including power, exponential, logarithmic, trigonometric and inverse trigonometric functions  
• Derivative rules for sums, products and quotients of functions  
• Chain rule and implicit differentiation  
 **Interpretations and properties of definite integrals**

• Definite integral as a limit of Riemann sums.

• Definite integral of the rate of change of a quantity over an interval interpreted as the change of the quantity over the interval

• Basic properties of definite integrals (examples include additivity and linearity).

**\* Applications of integrals.**

**Fundamental Theorem of Calculus**

• Use of the Fundamental Theorem to evaluate definite integrals.

• Use of the Fundamental Theorem to represent a particular antiderivative, and the analytical and graphical analysis of functions so defined.

**Techniques of antidifferentiation**

• Antiderivatives following directly from derivatives of basic functions.

• Antiderivatives by substitution of variables (including change of limits for definite integrals)

•L’Hospital’s Rule, including its use in determining limits

**Applications of antidifferentiation**

• Finding specific antiderivatives using initial conditions, including applications to motion along a line

• Solving separable differential equations and using them in modeling (including the study of the equation *y* = *ky* and exponential growth)

**Numerical approximations to definite integrals.** Use of Riemann sums (using left, right and midpoint evaluation points) and trapezoidal sums to approximate definite integrals of functions represented algebraically, graphically and by tables of values

**Grading**

* Summative 80% (including, but not limited to…)
  + Tests
  + Quizzes
  + Problem Sets/Graded Worksheets
  + Group Work
  + Projects
* Formative 20% (including, but not limited to…
  + Skills quizzes
  + Test corrections (where assigned)