

# Modeling Trig Functions

DAY 7

## 1. Write a sine and cosine equation of the function.

Step 1: Draw the middle line.

Step 2: Find a and d.

Step 3: Write the period formula.

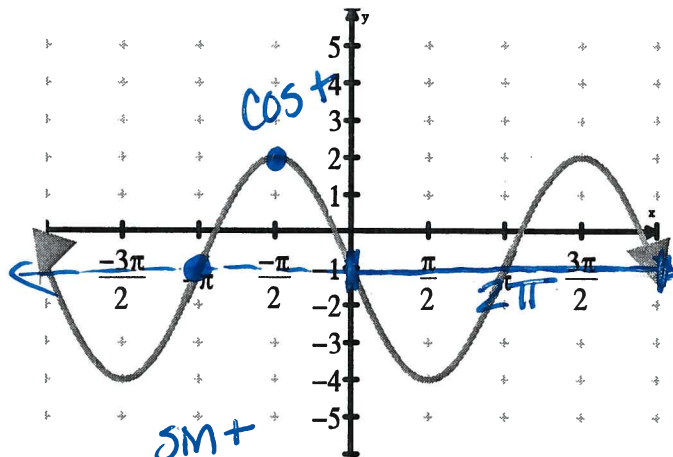
Find the period on the graph.

(measure from the y-axis).

Solve for b.

$$a = 3$$

$$d = -1$$



Step 4: Choose a starting point (sine is in the middle, cosine is low or high)

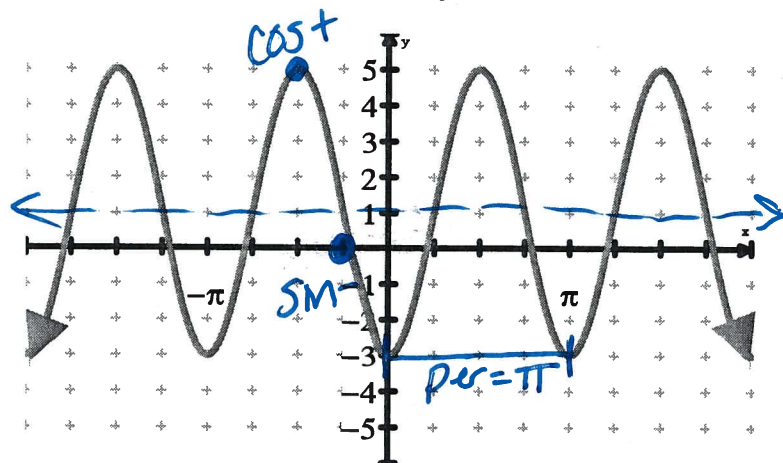
Step 5: Determine if a will be positive or negative based on the starting point.

Step 4: Write  $(bx - c) = 0$  and substitute b. Find the phase shift on the graph and substitute it for x. Then solve for c.

Step 5: Write the function!

Sine	Cosine
$y = a \sin(bx - c) + d$ $y = 3 \sin(bx - c) - 1$	$y = a \cos(bx - c) + d$ $y = 3 \cos(bx - c) - 1$
$\frac{2\pi}{b} = 2\pi \quad \left  \quad \begin{array}{l} bx - c = 0 \\ 1(-\pi) - c = 0 \\ -\pi = c \end{array} \right.$	$\frac{2\pi}{b} = 2\pi \quad \left  \quad \begin{array}{l} bx - c = 0 \\ 1(-\frac{\pi}{2}) - c = 0 \\ -\frac{\pi}{2} = c \end{array} \right.$
$b = 1$	$b = 1$
$y = 3 \sin(1x + \pi) - 1$	$y = 3 \cos(1x + \frac{\pi}{2}) - 1$

2. Write a sine and cosine equation of the function below.

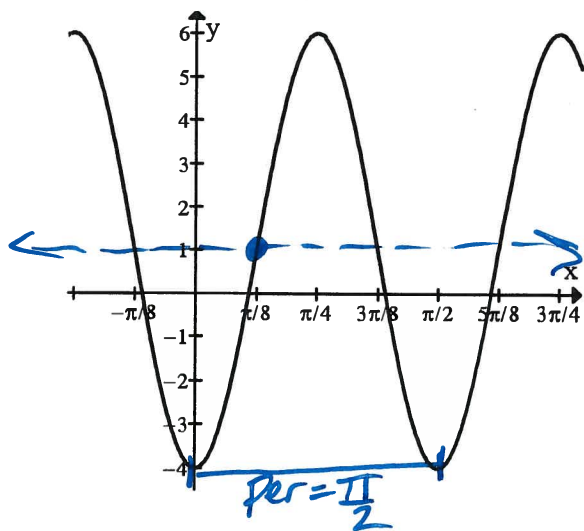


$$a = 4$$

$$d = 1$$

Sine	Cosine
$y = 4 \sin (bx - c) + 1$ $\frac{2\pi}{b} = \pi \quad   \quad bx - c = 0$ $\frac{2\pi}{\pi} = \frac{b\pi}{\pi} \quad   \quad 2(-\frac{\pi}{4}) - c = 0$ $b = 2 \quad   \quad -\frac{\pi}{2} = c$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <math display="block">y = -4 \sin (2x + \frac{\pi}{2}) + 1</math> </div>	$y = 4 \cos (bx - c) + 1$ $b = 2 \quad   \quad bx - c = 0$ $2(-\frac{\pi}{2}) - c = 0$ $-\pi = c$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <math display="block">y = 4 \cos (2x + \pi) + 1</math> </div>

3. Write a sine equation of the function below.



$$a = 5$$

$$d = 1$$

$$y = 5 \sin (bx - c) + 1$$

$$\frac{2\pi}{b} = \frac{\pi}{2} \quad | \quad bx - c = 0$$

$$\frac{4\pi}{\pi} = \frac{b\pi}{\pi} \quad | \quad 4(\frac{\pi}{8}) - c = 0$$

$$b = 4$$

$$\frac{\pi}{2} = c$$

$$y = 5 \sin (4x - \frac{\pi}{2}) + 1$$