

Bell Ringer

Grab a large notecard - put your name on it:

Look in your notes and put:

- ~ all equations of a line (4 forms)
- ~ slope formula for a line
- ~ information about parallel & perpendicular lines
- ~ root form of a parabola
- ~ vertex form of a parabola

$$y = mx + b$$

$$y - y_1 = m(x - x_1)$$

$$Ax + By = C$$

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

|| lines have same slope
 ⊥ lines have opposite reciprocal
 $\frac{3}{4} \perp \rightarrow -\frac{4}{3}$

parabolas

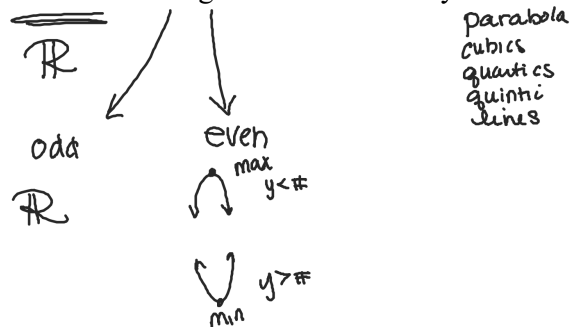
root form
 $y = a(x - r_1)(x - r_2)$

vertex
 $y = a(x - h)^2 + k$

Agenda

- Bell Ringer Answers ✓
- Review: Domain & Range of Functions
- Notes: Composites $f(g(x))$
- Domain & Range of Composites
- CW: If I were the teacher...
- Closure
- HW Time (?)

Domain & Range of Functions: Polynomials



Domain & Range of Functions: Square Roots

$$y = \sqrt{x}$$

$$y = \sqrt{x-7}$$

No -#s in $\sqrt{\quad}$
 Domain: $x \geq 0$
 $x \geq 0$

D: $x-7 \geq 0$
 $x \geq 7$

Range: plug back into original
 $y \geq 0$

$y = \sqrt{x} + 3$
 D: $x \geq 0$
 R: $y \geq 3$

Domain & Range: Rational Functions (Fractions)

cannot divide by 0

$$\frac{1}{x}$$

$x \neq 0$

$$\frac{1}{x+52}$$

$x+52 \neq 0$
 $x \neq -52$

$$\frac{1}{x^2-4}$$

$x^2-4 \neq 0$
 $(x+2)(x-2) \neq 0$
 $x \neq 2 \quad x \neq -2$

Domain & Range: Exponents & Logarithms



D: \mathbb{R}
 R: $y > 0$



D: $x > 0$
 R: \mathbb{R}

Composites

$$f \circ g(x) \rightarrow f(g(x))$$

$\rightarrow x$ must be in the D of $g(x)$

$\rightarrow g(x)$ must be in the D of $f(x)$

$$f(g(7)) = f(14)$$

$$f(x) = 4x^2 - 2x$$

$$4(14)^2 - 2(14)$$

$$756$$

$$f(g(x)) = f(ax)$$

$$4(ax)^2 - 2(ax)$$

$$4(4x^2) - 4x = 16x^2 - 4x$$

$g(x) = 2x$
 $a: 7=14$

$$f(x) = \textcircled{0}^2 + \textcircled{x}$$

\mathbb{R}

$$g(x) = \textcircled{x} + 1$$

\mathbb{R}

$$\begin{aligned} f(g(x)) &= f(x+1) \\ &= (x+1)^2 + (x+1) \\ &= (x+1)(x+1) + x+1 \\ &= x^2 + x + x + 1 + x + 1 \\ &= x^2 + 3x + 2 \quad \mathbb{R} \end{aligned}$$

$$g(f(x)) = g(x^2 + x) = \begin{matrix} (x^2 + x) + 1 \\ x^2 + x + 1 \end{matrix} \quad \mathbb{R}$$

$$f(x) = x^3 \quad \mathbb{R}$$

$$g(x) = \sqrt{x} \quad x \geq 0$$

$$h(x) = x - 4 \quad \mathbb{R}$$

$$j(x) = 2x \quad \mathbb{R}$$

$$f(h(x))$$

$$f(x-4)$$

$$(x-4)^3$$

$$(x^2 - 8x + 16)(x-4)$$

$$x^3 - 4x^2 - 8x^2 + 32x + 16x - 64$$

$$x^3 - 12x^2 + 48x - 64 \quad \mathbb{R}$$

$$\begin{matrix} j(f(x)) \\ j(x^3) \\ 2x^3 \\ \mathbb{R} \end{matrix}$$

$$f(x) = x^3$$

$$h(x) = x - 4$$

$$g(h(x))$$

$$g(x-4)$$

$$\sqrt{x-4}$$

$$\begin{matrix} x-4 \geq 0 \\ x \geq 4 \end{matrix}$$

$$g(x) = \sqrt{x}$$

$$j(x) = 2x$$

$$j(g(x))$$

$$j(\sqrt{x}) = 2\sqrt{x}$$

$$x \geq 0$$

$$f(x) = x^3$$

$$h(x) = x - 4$$

$$g(f(x))$$

$$g(x^3)$$

$$\sqrt{x^3}$$

$$x^3 \geq 0$$

$$x \geq 0$$

$$g(x) = \sqrt{x}$$

$$j(x) = 2x$$

$$g(j(x)) = g(2x)$$

$$\sqrt{2x}$$

$$\sqrt{2x}$$

$$2x \geq 0$$

$$x \geq 0$$

If I were the teacher...

On a sheet of paper: write a question that would be a good quiz questions.

- ~ composite - create two functions
- ~ be able to find the domain of each
- ~ pick a combination
- ~ find the domain of the composite

Why is this a good quiz questions?

Too easy? Too hard? Take too long?

$$f(x) = x^2 + x \quad g(x) = \sqrt{x+1}$$

$$f(g(x))$$

$$f(x+1) = (x+1)^2 + (x+1)$$

$$g(f(x)) = \sqrt{x^2 + x + 1}$$

Closure

Think about the domain of a function.

Partner A: Explain how to find the domain of a square root.
Victor

Partner B: Explain how to find the domain of a rational function.
Marvin

Partner A: Explain how to find the domain of an exponential function.
Tess

Partner B: Explain how to find the domain of a logarithmic function.
Donnie

Be prepared to share