## Released Test

## GEOMETRY

# 2009 Mathematics Standards of Learning 

Released Spring 2014

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## SAMPLE A

For what value of $x$ is $\triangle A B C \sim \triangle D E F$ ?
A 18B 21C 25

D 72

Directions: Type your answer in the box.

## SAMPLE B

What is the total number of lines of symmetry for this figure?


Let $p$ represent
Two angles are vertical angles.
Let $q$ represent
The angles are congruent.
What is the symbolic representation of the following statement?
If two angles are congruent, then the angles are vertical angles.A $q \rightarrow p$B $p \rightarrow q$C $\sim q \rightarrow \sim p$D $\sim p \rightarrow \sim q$

## Beth is drawing the perpendicular bisector of $\overline{S T}$.



Which point is on the perpendicular bisector of $\overline{S T}$ ?A $W$

B $X$c $Y$

D $Z$

In this figure, parallel lines $a$ and $b$ are intersected by line $c$.


Which pair of angles is NOT supplementary?A $\angle 1$ and $\angle 6$
B $\angle 3$ and $\angle 8$C $\angle 2$ and $\angle 7$D $\angle 4$ and $\angle 6$

## What type of construction is illustrated in the figure?

A The bisection of $\angle D$B The bisection of $\overline{B D}$C An angle congruent to $\angle D$D A line segment congruent to $\overline{A B}$

This Venn diagram represents students who play instruments in the orchestra.


Identify each region of the Venn diagram that represents students who play only the flute and the oboe.

An angle congruent to angle $\boldsymbol{A}$ is being constructed.


Which ray could be drawn to construct an angle congruent to $\angle A$ ?A $\overrightarrow{B C}$B $\overrightarrow{B D}$C $\overrightarrow{B E}$D $\overrightarrow{B F}$

Which diagram shows a pair of angle measures that prove lines $a$ and $b$ are parallel?
-
C




Which is a valid conclusion that can be drawn from these statements?
If a quadrilateral is a rhombus, then it is a parallelogram.
If a quadrilateral is a parallelogram, then its opposite angles are congruent.A Every quadrilateral is a rhombus.B Every parallelogram is a rhombus.C Opposite angles of a rhombus are congruent.D Opposite angles of a quadrilateral are congruent.

This figure shows parallel stair railings through points $M, N, P$, and $Q$.


What is the value of $x$ ?A 29B 45C 61D 119

Given: $S(-1,8)$ and $T(7,-9)$


What is the length of $\overline{S T}$ ?A $\sqrt{23}$B 5C $5 \sqrt{13}$D $\sqrt{353}$

Directions: Click on the grid to plot the point you want to select. You must plot a point other than point $P$.

Line $t$ contains the points $(-8,5)$ and $(8,-3)$. Plot a point other than point $P$ with integral coordinates that is on a line parallel to $t$ and passes through point $P$.


Which best describes the construction in the diagram shown?
A The bisector of a line segmentB A line segment congruent to a given line segmentC A perpendicular to a given line at a point on the lineD A perpendicular to a given line from a point not on the line

## Which is the inverse of the following statement?

If the measure of an angle is $90^{\circ}$, then it is a right angle.A If the measure of an angle is not $90^{\circ}$, then it is not a right angle.B If the measure of an angle is not $90^{\circ}$, then it is a right angle.C If an angle is not a right angle, then its measure is not $90^{\circ}$.D If an angle is a right angle, then its measure is $90^{\circ}$.

Quadrilateral TUVW is shown.


If $T U V W$ is reflected across the line $y=x$, what are the coordinates of $V^{\prime} ?$A $(8,-3)$B $(3,8)$C $(-3,-8)$D $(-8,3)$

Directions: Type your answer in the box.

Lines $r$ and $s$ are cut by a transversal.


What value of $x$ proves that $r \| s$ ?

$$
x=1
$$

## Given: $P(5,7)$ and $T(-3,3)$

What is the slope of $\stackrel{\leftrightarrow}{P T}$ ?A -2
B $\frac{-1}{2}$

C $\frac{1}{2}$

D 2

$$
\text { For which polygon are both } x=-1 \text { and } y=-2 \text { lines of symmetry? }
$$

A

C

B

D


The figure represents a ramp with handrails. Segments $A B$ and $D E$ are parallel to $\overline{G H}$. Segments $B C$ and $E F$ are parallel to $\overline{H J}$. Segments $A G$ and $B H$ are parallel to $\overline{C J}$.


If $m \angle J C B=115^{\circ}$, what is $m \angle C B A$ ?A $65^{\circ}$B $90^{\circ}$C $115^{\circ}$D $155^{\circ}$

Reuben attached a wire between two poles on a hill as shown.


Which is closest to $x$, the distance between the two poles?A 27 ftB 29 ftC 60 ftD 75 ft

Triangles $A B E, A D E$, and $C B E$ are shown on the coordinate grid, and all the vertices have coordinates that are integers.


Which statement is true?A No two triangles are congruent.B Only $\triangle A B E$ and $\triangle C B E$ are congruent.C Only $\triangle A B E$ and $\triangle A D E$ are congruent.D Triangle $A B E, \triangle A D E$, and $\triangle C B E$ are all congruent.

Directions: Click and drag each selected number to the correct box.

The lengths of two sides of a triangle are $\mathbf{2 4}$ inches and 43 inches. What is the range of possible lengths, in inches, for the third side, $x$, of this triangle?


Which of the following sets of lengths can represent the measures of the sides of a right triangle?A $4,5,6$B 5, 12, 15C $8,10,17$D 20, 21, 29

Given the measures shown in the diagram, which two triangles are congruent?
A Q and SB R and TC R and SD Q and T

Part of a marching band formed a triangle made with trumpet players on one side, clarinet players on one side, and flute players on the third side.

- The angle formed by the trumpet and flute players measured $45^{\circ}$.
- The angle formed by the flute and clarinet players measured $68^{\circ}$.

Which orders the sides of this triangle from least to greatest using the instrument names?A Clarinet, trumpet, fluteB Clarinet, flute, trumpetC Trumpet, flute, clarinetD Flute, trumpet, clarinet

An equilateral triangle is folded in half.


What is $x$, the height of the equilateral triangle?A $14 \sqrt{3} \mathrm{~cm}$
B 14 cmC $7 \sqrt{3} \mathrm{~cm}$D 7 cm

Look at this triangle.


Which triangle is similar to the given triangle?
D


Directions: Click and drag each selected reason to the correct box.

Given: Figure $A B C D$ with diagonal $\overline{A C}$

$$
\overline{A B} \cong \overline{D C} ; \overline{B C} \cong \overline{A D}
$$



Complete the proof of $\triangle A B C \cong \triangle C D A$ by selecting the reasons for the last two statements.


A spectator is viewing the six cars of a roller coaster as it travels down a hill at an amusement park.


Which is closest to the total length of the six cars?A 12.3 ftB 15.8 ftC 25.6 ftD 32.5 ft

Three triangles that do not overlap are shown on the coordinate grid. The coordinates of all vertices are integers.


Which statement is true?A $\triangle A B D \sim \triangle E B A$B $\triangle A B D \sim \triangle D B C$C $\triangle C B D \sim \triangle A B E$D $\triangle C B D \sim \triangle E B A$


Using the information given, which congruence postulate or theorem can be used to prove that $\triangle P Q R \cong \triangle T S R$ ?A Side-Side-Side PostulateB Side-Angle-Side PostulateC Hypotenuse-Leg TheoremD Angle-Angle-Side Theorem

Which could be the lengths of three sides of a triangle?A $6 \mathrm{~cm}, 14 \mathrm{~cm}, 8 \mathrm{~cm}$B $9 \mathrm{~cm}, 11 \mathrm{~cm}, 21 \mathrm{~cm}$C $8.5 \mathrm{~cm}, 17 \mathrm{~cm}, 10.6 \mathrm{~cm}$D $14 \mathrm{~cm}, 4.7 \mathrm{~cm}, 4.7 \mathrm{~cm}$

Given: $Q$ lies on $\overline{P R}$ and $S$ lies on $\overline{R T}$


Which condition proves $\triangle P R T \sim \triangle Q R S$ ?
A $\angle P Q S \cong \angle T S Q$B $\angle P T R \cong \angle T P R$
c $\frac{Q S}{P T}=\frac{Q R}{S R}$D $\frac{Q R}{P R}=\frac{S R}{T R}$

Directions: Type your answer in the box.

Given: Parallelogram $Q R S T$ where $Q R=6 x-5$ and $R S=4 x+13$


What value of $x$ proves this parallelogram is a rhombus?

$$
x=
$$

The floor plan for a modern home is modeled by the composite of the regular nonagon and triangle shown.


What is the measure of $\angle J K L$ ?A $150^{\circ}$B $160^{\circ}$C $165^{\circ}$D $175^{\circ}$

Given: Circle $P$ with center at $(-4,1)$

Which equation could represent circle $P$ ?A $(x-4)^{2}+(y-1)^{2}=41$B $(x-4)^{2}+(y+1)^{2}=41$C $(x+4)^{2}+(y-1)^{2}=41$D $(x+4)^{2}+(y+1)^{2}=41$

This container is composed of a right circular cylinder and a right circular cone.


Which is closest to the surface area of the container?A $490 \mathrm{ft}^{2}$B $754 \mathrm{ft}^{2}$C $1,243 \mathrm{ft}^{2}$D $1,696 \mathrm{ft}^{2}$

Given: Circle $J$


What is the value of $y$ ?A 38B 50
C 88
D 92

A cell phone box in the shape of a rectangular prism is shown. The height of the box is $\mathbf{4} \mathbf{~ c m}$.


The height of the original box will be increased by 3.5 centimeters so a new instruction manual and an extra battery can be included. Which is closest to the total surface area of the new box?A $479 \mathrm{~cm}^{2}$B $707 \mathrm{~cm}^{2}$C $738 \mathrm{~cm}^{2}$D $959 \mathrm{~cm}^{2}$

Parallelogram $A B C D$ is a rhombus with $m \angle E B C=36^{\circ}$.


What is the $m \angle D A E$ ?A $36^{\circ}$B $54^{\circ}$C $108^{\circ}$D $144^{\circ}$

Circle $O$ has a center at $(-2,-2)$ and a diameter of 10 units.

Which point lies on circle $O$ ?A $(-6,-5)$
B $(-2,-2)$
C $(6,4)$
D $(8,8)$

An architect used this diagram to design a curved balcony. She drew a circle with a radius of 40 feet and a central angle of $70^{\circ}$ to determine the length of railing needed for the balcony.


Which is closest to the length of railing needed for the curved section of the balcony?A 24 ftB 49 ftC 251 ftD 977 ft

A polygon is shown.


What is the measure of $\angle U$ ?A $60^{\circ}$B $90^{\circ}$C $120^{\circ}$D $240^{\circ}$

The volume of a cube is $\mathbf{6 4}$ cubic centimeters. What is the surface area of the cube?A $16 \mathrm{~cm}^{2}$B $96 \mathrm{~cm}^{2}$C $256 \mathrm{~cm}^{2}$
D $384 \mathrm{~cm}^{2}$

The diagonals of rectangle $K L M N$ intersect at the point $(2,1)$. One of the vertices of rectangle $K L M N$ is located at $(-4,5)$.


Which of the following could be the location of another vertex of this rectangle?A $(8,-3)$B $(3,-1)$C $(-2,3)$D $(-10,9)$

Given: Circle $P$


Which is closest to the area of the shaded sector of circle $P$ ?A $11 \mathrm{~cm}^{2}$B $28 \mathrm{~cm}^{2}$C $50 \mathrm{~cm}^{2}$D $78 \mathrm{~cm}^{2}$

Directions: Click and drag each selected number to the correct box.

The ratio of the lengths of the radii of two spheres is $3: 5$. What is the ratio of the volumes of these two spheres?


| 1 | 3 | 5 | 9 | 15 | 25 | 27 | 125 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

This figure is composed of an isosceles trapezoid and a regular octagon.


What is the value of $x$ ?A 100B 125C 135D 190

Directions: Click on the grid to plot the point you want to select.

Plot the center of the circle defined by the equation $(x+4)^{2}+(y-5)^{2}=3^{2}$.


## A rectangular pyramid is shown.



What is the volume of the pyramid?A $864 \mathrm{~cm}^{3}$B $432 \mathrm{~cm}^{3}$C $288 \mathrm{~cm}^{3}$D $108 \mathrm{~cm}^{3}$

A company is creating a new cylindrical container to replace its original cylindrical container.

- The new container will have 4 times the volume of the original container.
- The height of the new container will remain the same as the height of the original container.

The length of the radius of the new container will be -A 2 times the length of the radius of the original containerB 4 times the length of the radius of the original containerC 8 times the length of the radius of the original containerD 16 times the length of the radius of the original container

## Geometry

## Released Test Spring 2014

Answer Key

| Sequence <br> Number | Item Type: Multiple Choice (MC) or <br> TechnologyEnhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 1 | MC | A | 001 | Reasoning, Lines, and Transformations |
| 2 | MC | B | 001 | Reasoning, Lines, and Transformations |
| 3 | MC | C | 001 | Reasoning, Lines, and Transformations |
| 4 | MC | A | 001 | Reasoning, Lines, and Transformations |
| 5 | TEI | The region that is common to both the Oboe circle and the Flute circle, but no other circle, as shown in the image below. This region, and only this region, must contain a star. <br> Directions: Click on the diagram to place $\mathbf{a}^{\text {" }}$ " in each region you want to select. You must select all correct regions. <br> This Venn diagram represents students who play instruments in the orchestra. <br> Identify each region of the Venn diagram that represents students who play only the flute and the oboe. | 001 | Reasoning, Lines, and Transformations |
| 6 | MC | A | 001 | Reasoning, Lines, and Transformations |
| 7 | MC | B | 001 | Reasoning, Lines, and Transformations |


| Sequence <br> Number | Item Type: <br> Multiple Choice (MC) or <br> TechnologyEnhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 8 | MC | C | 001 | Reasoning, Lines, and Transformations |
| 9 | MC | C | 001 | Reasoning, Lines, and Transformations |
| 10 | MC | D | 001 | Reasoning, Lines, and Transformations |
| 11 | TEI | Any ONE of these points must be plotted on the coordinate plane: $(10,-9),(8,-8),(6,-7),(2,-5),(0,-4),(-2,-3),(-4,-2),(-6,-1)$, $(-8,0)$ or $(-10,1)$ <br> One of these points, $(2,-5)$, is shown on the coordinate plane below. <br> Directions: Click on the grid to plot the point you want to select. You must plot a point other than point $\boldsymbol{P}$. <br> Line $t$ contains the points $(-8,5)$ and $(8,-3)$. Plot a point other than point $P$ with integral coordinates that is on a line parallel to $t$ and passes through point $P$. | 001 | Reasoning, Lines, and Transformations |
| 12 | MC | D | 001 | Reasoning, Lines, and Transformations |
| 13 | MC | A | 001 | Reasoning, Lines, and Transformations |
| 14 | MC | D | 001 | Reasoning, Lines, and Transformations |


| Sequence <br> Number | Item Type: <br> Multiple Choice <br> (MC) or <br> Technology- <br> Enhanced Item <br> (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 15 | TEI | Typed Response: 43 (and all equivalent answers) | 001 | Reasoning, Lines, and Transformations |
|  |  | Directions: Type your answer in the box. |  |  |
|  |  | Lines $r$ and $s$ are cut by a transversal.What value of $x$ proves that $r \\| s$ ? |  |  |
|  |  |  |  |  |
|  |  | 43 |  |  |
| 16 | MC | C |  |  |
| 17 | MC | C | 001 | Reasoning, Lines, and Transformations |
| 18 | MC | D | 001 | Reasoning, Lines, and Transformations |
| 19 | MC | D | 002 | Triangles |
| 20 | MC | D | 002 | Triangles |


| Sequence <br> Number | Item Type: <br> Multiple Choice (MC) or <br> TechnologyEnhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 21 | TEI | The number 19 must be placed in the box on the left, and the number 67 must be placed in the box on the right. <br> Directions: Click and drag each selected number to the correct box. <br> The lengths of two sides of a triangle are 24 inches and 43 inches. What is the range of possible lengths, in inches, for the third side, $x$, of this triangle? $\square$ $<x<$ $\square$ | 002 | Triangles |
| 22 | MC | D | 002 | Triangles |
| 23 | MC | A | 002 | Triangles |
| 24 | MC | B | 002 | Triangles |
| 25 | MC | C | 002 | Triangles |
| 26 | MC | A | 002 | Triangles |


| Sequence Number | Item Type: <br> Multiple Choice (MC) or <br> TechnologyEnhanced Item (TEI) | Correct Answer |  |  | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 27 | TEI | "Reflexive Property" must of the table; "Side-Side-Si row, second column of the <br> Directions: Click and drag each selected re <br> Given: Figure $A B C D$ with diagon $\overline{A B} \cong \overline{D C} ; \overline{B C} \cong \overline{A D}$ <br> Complete the proof of $\triangle A B C \cong \triangle$ <br> Statements | placed in (SSS) The ble. <br> n to the correct box <br> $\bar{C}$ <br> $A$ by selecting th | cond row, second column ' must be placed in the third <br> or the last two statements. | 002 | Triangles |
| 28 | MC |  | D |  | 002 | Triangles |
| 29 | MC |  | C |  | 002 | Triangles |
| 30 | MC |  | D |  | 002 | Triangles |
| 31 | MC |  | C |  | 002 | Triangles |
| 32 | MC |  | D |  | 002 | Triangles |


| Sequence <br> Number | Item Type: Multiple Choice (MC) or <br> TechnologyEnhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 33 | TEI | Typed response: 9 (and all equivalent answers) <br> Directions: Type your answer in the box. <br> Given: Parallelogram $Q R S T$ where $Q R=6 x-5$ and $R S=4 x+13$ <br> What value of $x$ proves this parallelogram is a rhombus? $x=9$ | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 34 | MC | B | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 35 | MC | C | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 36 | MC | D | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 37 | MC | A | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 38 | MC | D | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 39 | MC | B | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 40 | MC | A | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 41 | MC | B | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 42 | MC | C | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 43 | MC | B | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 44 | MC | A | 003 | Polygons, Circles, and Three-Dimensional Figures |


| Sequence <br> Number | Item Type: <br> Multiple Choice (MC) or <br> TechnologyEnhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 45 | MC | B | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 46 | TEI | The numbers 27 and 125 should be placed in the boxes. The order of the numbers in the boxes does not matter, since this question did not specifically state the order in which the volumes of the two spheres should be compared. <br> Directions: Click and drag each selected number to the correct box. <br> The ratio of the lengths of the radii of two spheres is $3: 5$. What is the ratio of the volumes of these two spheres? $\square$ | 003 | Polygons, Circles, and Three-Dimensional Figures |
| 47 | MC | A | 003 | Polygons, Circles, and Three-Dimensional Figures |



| Total Raw Score If you get this many items correct: | Total Scaled Score <br> Then your converted scaled score is: |
| :---: | :---: |
| 0 | 0 |
| 1 | 223 |
| 2 | 254 |
| 3 | 273 |
| 4 | 287 |
| 5 | 298 |
| 6 | 308 |
| 7 | 316 |
| 8 | 323 |
| 9 | 330 |
| 10 | 336 |
| 11 | 341 |
| 12 | 347 |
| 13 | 352 |
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| 31 | 425 |
| 32 | 430 |
| 33 | 434 |
| 34 | 438 |
| 35 | 443 |
| 36 | 447 |
| 37 | 452 |
| 38 | 457 |
| 39 | 462 |
| 40 | 468 |
| 41 | 474 |
| 42 | 480 |
| 43 | 487 |
| 44 | 495 |
| 45 | 505 |
| 46 | 516 |
| 47 | 529 |
| 48 | 548 |
| 49 | 579 |
| 50 | 600 |

A total raw score (left
column) is converted to total scaled score (right column). The total scaled score may range from 0 to 600.

A scaled score of 400 or more means the student passed the SOL test, while a scaled score of 399 or less means the student did not pass the test. A scaled score of 500 or more indicates the student passed the SOL test at an advanced level

