## Released Test

## ALGEBRA II

# 2009 Mathematics Standards of Learning 

Released Spring 2014

## Property of the Virginia Department of Education

Copyright ©2014 by the Commonwealth of Virginia, Department of Education, P.O. Box 2120, Richmond, Virginia 23218-2120. All rights reserved. Except as permitted by law, this material may not be reproduced or used in any form or by any means, electronic or mechanical, including photocopying or recording, or by any information storage or retrieval system, without written permission from the copyright owner. Commonwealth of Virginia public school educators may reproduce any portion of these released tests for non-commercial educational purposes without requesting permission. All others should direct their written requests to the Virginia Department of Education, Division of Student Assessment and School Improvement, at the above address or by e-mail to Student_Assessment@doe.virginia.gov

## SAMPLE A

Which expression is equivalent to $\sqrt{\frac{7 x}{16}}$ ?
A $\frac{7 x}{4}$

B $\frac{7 x}{8}$

C $\frac{\sqrt{7 x}}{4}$

D $\frac{\sqrt{7 x}}{8}$

Directions: Type your answer in the box.

## SAMPLE B

What value of $x$ makes $\sqrt{x}-3=6$ true?


Which expression is equivalent to $\frac{3 n}{n+3}+\frac{5}{n-4}$ if no denominator equals zero?
A $\frac{3 n^{2}-7 n+3}{(n+3)(n-4)}$

B $\frac{3 n^{2}-7 n+15}{(n+3)(n-4)}$
c $\frac{3 n^{2}+5 n+3}{(n+3)(n-4)}$

D $\frac{3 n^{2}+5 n+15}{(n+3)(n-4)}$

Which number is equivalent to $(-6-i)+5 i-(11+13 i)$ ?A $-17-9 i$
B $-17+17 i$C $-5-9 i$D $-5+17 i$

Which of the following is the factored form of $x^{3}-216$ ?
A $(x-6)^{3}$B $(x-6)\left(x^{2}+36\right)$C $(x-6)\left(x^{2}+12 x+36\right)$D $(x-6)\left(x^{2}+6 x+36\right)$

Which expression is equivalent to $\sqrt{75 x^{3}}-\sqrt{27 x^{3}}$, if $x>0$ ?A $4 x \sqrt{6 x}$
B $4 x \sqrt{3 x}$C $2 x \sqrt{6 x}$
D $2 x \sqrt{3 x}$

Assuming that no denominator equals zero, which is equivalent to $\frac{r^{2}-r-6}{(r-2)(r-3)}$ ?
A $\frac{r+2}{r-2}$
B $\frac{r+3}{r-3}$
c $\frac{r+2}{r-1}$
D $\frac{2(r-1)}{r-2}$

Which expression is equivalent to $\sqrt[4]{16 x^{15} y^{17}}$, where $x>0$ and $y>0$ ?A $4 x^{11} y^{13}$
B $4 x^{\frac{15}{4}} y^{\frac{17}{4}}$C $2 x^{11} y^{13}$D $2 x^{\frac{15}{4}} y^{\frac{17}{4}}$

Which is equivalent to $(6+\sqrt{7})(5+\sqrt{7})$ ?
A $11+2 \sqrt{7}$
B $30+11 \sqrt{7}$
C $30+18 \sqrt{7}$
D $37+11 \sqrt{7}$

Directions: Click and drag each selected term to the correct box.

Simplify completely: $\sqrt[3]{162 x^{6} y^{7}}$


Which expression is equivalent to $x^{\frac{3}{7}} y^{\frac{36}{7}}$ ?
A $\frac{1}{7} \sqrt{x^{3} y^{36}}$
B $\frac{1}{7} y^{5} \sqrt{x^{3} y}$
c $y^{5} \sqrt[7]{x^{3} y}$D $x^{3} y^{5} \sqrt[7]{y}$

Directions: Click and drag each selected binomial to the box.

Factor the following polynomial.

$$
8 x^{2}-18 x y-5 y^{2}=\square
$$

$$
\begin{array}{|l|l|l|l|l|l|}
\hline(x+5 y) & (2 x-5 y) & (2 x-y) & (4 x+y) & (4 x+5 y) & (8 x-y) \\
\hline
\end{array}
$$

Which statement illustrates the symmetric property of equality?A If $7 \sqrt{x}+17 i=49 i$, then $7 \sqrt{x}+17 i=49 i$.B If $7 \sqrt{x}+17 i=49 i$, then $49 i=7 \sqrt{x}+17 i$.C If $7 \sqrt{x}+17 i=49 i$ and $49 i=12 \sqrt{x}-3 i$, then $7 \sqrt{x}+17 i=12 \sqrt{x}-3 i$.D If $7 \sqrt{x}+17 i=49 i$ and $7 \sqrt{x}+17 i-y=-35 i$, then $49 i-y=-35 i$.

Directions: Click on the box to choose each expression you want to select. You must select all the correct expressions.

Identify each expression that is equivalent to (i).

| $i^{47}$ | $i^{33}$ | $i^{21}$ | $i^{15}$ |
| :--- | :--- | :--- | :--- |

Given:

$$
\frac{\frac{n-15}{9 n}}{\frac{15-n}{3 n^{5}}}
$$

Assuming no denominator equals zero, which expression is equivalent to the given expression?A $\frac{-n^{4}}{3}$
B $\frac{n^{4}}{3}$C ${ }^{-} \frac{3}{n^{4}}$
D $\frac{3}{n^{4}}$

What is the solution set of $\sqrt{8 x-1}+4=8$ ?
A $\left\{\frac{67}{8}\right\}$
B $\left\{\frac{61}{8}\right\}$
C $\left\{\frac{17}{8}\right\}$
D $\left\{\frac{15}{8}\right\}$

Which graph best represents the solution for $y \geq|2 x+1|-3$ ?

$\bigcirc \mathbf{C}$
B

○


What is the solution set to $x^{2}=16-4 x$ ?


What is the solution set for $\sqrt[3]{\frac{1}{4} x+3}=2$ ?
A $\left\{\frac{5}{4}\right\}$
B $\left\{\frac{11}{4}\right\}$C $\{20\}$D $\{44\}$

What is the solution to $|x+4|<2$ ?
A $x<-6$ or $x>-2$
B $-6<x<-2$
C $x<-2$
D $2<x<6$

## The graph of $g(x)$ is shown.



Which appears to be a solution of $g(x)=0$ ?A -3B -1C 0D 3

Given: $\left\{\begin{array}{l}x+y+10=0 \\ x^{2}+y-2=0\end{array}\right.$

What are the $x$-values for the solutions to the given system of equations?A $x=-3,-7$
B $x=-3,4$C $x=-4,3$D $x=4,-14$

Which is a solution for $\sqrt[4]{w-4}+\mathbf{1 1}=14$ ?

A $w=8$
B $w=16$
C $w=77$
D $w=85$

Directions: Click on the grid to plot each point that is a solution. You must plot all correct solutions.

The graph of a system of two equations is shown on the grid. Identify only the apparent solutions to this system of equations.


Which is a solution to $\frac{4 n-37}{3}=\frac{10}{n}$, if $n \neq 0$ ?

A -10
B $\frac{-27}{4}$
C $\frac{-10}{11}$
D $\frac{-3}{4}$

Which is a solution of $|2 x-7|+1=9$ ?
A $x=\frac{17}{2}$
B $x=\frac{1}{2}$
C $x=\frac{-1}{2}$
D $x=\frac{-3}{2}$

Directions: Type your answer in the box.

If $x \neq 0$, what is the solution to the following equation?

$$
\begin{aligned}
& \frac{1-x}{x}+2=\frac{7}{x} \\
& x=
\end{aligned}
$$

A solution to a quadratic equation is $13-11 i \sqrt{7}$. Which of the following must also be a solution to this equation?A $-13-11 i \sqrt{7}$B $-13+11 i \sqrt{7}$C $13-11 i \sqrt{7}$D $13+11 i \sqrt{7}$

Which of the following functions does NOT have a range of only the real numbers greater than or equal to zero?A $f(x)=\sqrt{4-x}$B $f(x)=|x-4|$C $f(x)=x^{4}$D $f(x)=\log x$

Directions: Type your answer in the box.

What is the sum of this infinite series?

$$
100+60+36+\frac{108}{5}+\cdots
$$



The graph of a parent function is shown.


Which function belongs to this same family?A $g(x)=-\log (x-1)$
B $g(x)=\left(\frac{1}{3}\right)^{(x-1)}$C $g(x)=3^{(x-1)}$D $g(x)=\frac{3}{x-1}$

Which number is a zero of $f(x)=\log (4 x-1)$ ?

A $\frac{7}{2}$

B $\frac{11}{4}$
c $\frac{1}{2}$

D $\frac{1}{4}$

What is the equation of the horizontal asymptote of the graph of the following equation?

$$
f(x)=6^{(x-5)}-4
$$A $y=6$

B $y=0$
C $y=-4$D $y=-5$

Which function best represents this graph?
A $f(x)=2^{(x+2)}$B $f(x)=2^{(x-2)}$C $f(x)=2^{x}-3$D $f(x)=2^{x}-4$

The graph of $g(x)=\log (2 x)$ has -A no $x$-intercept or $y$-interceptB one $x$-intercept and no $y$-interceptC two $x$-intercepts and no $y$-intercept
D one $x$-intercept and one $y$-intercept

Throughout which of the following intervals is $f(x)=(x-1)(x-4)^{2}$ only decreasing?A $-\infty<x<0$
B $-\infty<x<1$C $1<x<4$D $2<x<4$

Given: $f(x)=\log (x-16)+15$

What is the equation of an asymptote of the graph of the given function?A $x=16$B $y=16$C $x=15$D $y=15$

The graph of a function is shown on the grid.


What appears to be the range of this function?A $\{y \mid y=1,2,3,4\}$B $\{y \mid y=0,2,4,6,8\}$C $\{y \mid 1<y<4\}$D $\{y \mid 0<y<8\}$

The heights of a large population of ostriches are normally distributed. Which is closest to the percentage of these heights that is within $\mathbf{3}$ standard deviations of the mean?A $0.3 \%$B 5\%C $95 \%$D 99.7\%

Which of these situations involves a combination?A Determining how many different groups of 3 employees can be chosen from 10 employeesB Determining how many different seating charts can be made placing 7 people around a tableC Determining how many different ways 8 runners can be assigned lanes on a track for a preliminary raceD Determining how many different 6-letter passwords can be made using the letters in the word "pencil"

What is the 14th term of the arithmetic sequence with a first term of $\mathbf{7}$ and a common difference of $\mathbf{1 0}$ ?

A 130B 137C 147D 221

The graph of the function $g$ is shown on the following grid.


Which graph best represents the inverse of $g$ ?
-

$\bigcirc$
B


- D


Directions: Click on a box to choose each ordered pair you want to select. You must select all correct ordered pairs.

Identify each of the $x$ - and $y$-intercepts of the function $h(x)=x^{3}+3 x^{2}-4 x-12$.

| $(-3,0)$ | $(0,-2)$ |
| :---: | :---: |
| $(-2,0)$ | $(0,0)$ |
| $(0,-12)$ | $(0,2)$ |
| $(0,-3)$ | $(2,0)$ |

Which of the following describes the end behavior of $y={ }^{-} x^{2}+b x+c$ as $x$ approaches either positive or negative infinity?A $y$ approaches positive infinityB $y$ approaches negative infinityC $y$ approaches $c$D $y$ approaches ${ }^{-} \frac{c}{b}$

If $f(x)=\frac{2}{3} x^{2}+1$ and $g(x)=6 x-15$, which polynomial is equivalent to $g(f(x))$ ?A $4 x^{2}-13$
B $4 x^{2}-9$C $4 x^{3}-10 x^{2}+6 x-15$D $16 x^{2}-80 x+101$

The domain of the function $f(x)=\frac{x+3}{x^{2}+5 x-24}$ is all real numbers except -

A $-8,-3,3$B $-8,3$
C $-3,8$D 8

The amount of work ( $W$ ) done when lifting an object varies jointly with the mass of the object $(M)$ and the distance the object is lifted ( $D$ ). Which equation models this relationship?

A $W=\frac{k}{M D}$B $W=\frac{k M}{D}$C $W=k M D$D $W=\frac{k D}{M}$

Madison deposited \$1,000 into a savings account that compounds interest yearly. After her initial deposit, Madison did not withdraw or deposit any money from this account. The table below shows the amount in her savings account over a period of years.

Amount in Savings Account

| Number of <br> Years After <br> the Deposit | Amount in <br> Savings |
| :---: | :---: |
| 2 | $\$ 1,123.60$ |
| 4 | $\$ 1,262.48$ |
| 6 | $\$ 1,418.52$ |
| 8 | $\$ 1,593.85$ |
| 10 | $\$ 1,790.85$ |

Using the exponential curve of best fit, which is closest to the expected amount in the savings account 30 years after the time Madison deposited the initial \$1,000 ?A $\$ 2,854$B $\$ 3,291$C $\$ 5,743$D $\$ 16,854$

Which graph best represents a function with zeros of $-2,-1$, and $2 ?$

A

©
B

D


The number of permutations of 8 objects taken $\mathbf{3}$ at a time is -
A 40,320B 6,720C 4,920D 336

If $y$ varies inversely as the square root of $x$, what is the constant of proportionality if $y=16$ when $x=4$ ?A 4
B 8C 32D 64

Which of the following describes the root(s) of the equation $9 x^{2}=6 x-1$ ?

A Exactly one real rootB Two distinct real rootsC Exactly one imaginary rootD Two distinct imaginary roots

Algebra II
Released Test Spring 2014
Answer Key

| Test Sequence Number | Item Type: Multiple Choice (MC) or Technology Enhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 1 | MC | B | 001 | Expressions and Operations |
| 2 | MC | A | 001 | Expressions and Operations |
| 3 | MC | D | 001 | Expressions and Operations |
| 4 | MC | D | 001 | Expressions and Operations |
| 5 | MC | A | 001 | Expressions and Operations |
| 6 | MC | D | 001 | Expressions and Operations |
| 7 | MC | D | 001 | Expressions and Operations |
| 8 | TEI | $3, x^{2}$, and $y^{2}$ should be placed in the box to the left of the radical sign. The order in which these are placed in this box does not matter. 6 and $y$ should be placed in the box to the right of the radical sign. The order in which these are placed in this box does not matter. <br> Directions: Click and drag each selected term to the correct box. <br> Simplify completely: $\sqrt[3]{162 x^{6} y^{7}}$ | 001 | Expressions and Operations |








| Test <br> Sequence <br> Number | Item Type: Multiple Choice (MC) or Technology Enhanced Item (TEI) | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: | :---: |
| 40 | MC | C | 003 | Functions and Statistics |
| 41 | TEI | $\begin{aligned} & (-3,0),(-2,0),(0,-12), \text { and }(2,0) \\ & \text { All four ordered pairs. and only these ordered pairs. must be selected. } \end{aligned}$ | 003 | Functions and Statistics |
|  |  | Directions: Click on a box to choose each ordered pair you want to select. You must select all correct ordered pairs. |  |  |
|  |  | Identify each of the $x$ - and $y$-intercepts of the function $h(x)=x^{3}+3 x^{2}-4 x-12$. |  |  |
|  |  | $(-3,0)$ $(0,-2)$ <br> $(-2,0)$ $(0,0)$ <br> $(0,-12)$ $(0,2)$ <br> $(0,-3)$ $(2,0)$ |  |  |
| 42 | MC | B | 003 | Functions and Statistics |
| 43 | MC | B | 003 | Functions and Statistics |
| 44 | MC | B | 003 | Functions and Statistics |
| 45 | MC | C | 003 | Functions and Statistics |
| 46 | MC | C | 003 | Functions and Statistics |
| 47 | MC | D | 003 | Functions and Statistics |
| 48 | MC | D | 003 | Functions and Statistics |
| 49 | MC | C | 003 | Functions and Statistics |
| 50 | MC | A | 003 | Functions and Statistics |


| Total Raw Score If you get this many items correct: | Total Scaled Score Then your converted scaled score is: |
| :---: | :---: |
| 0 | 0 |
| 1 | 159 |
| 2 | 198 |
| 3 | 222 |
| 4 | 239 |
| 5 | 253 |
| 6 | 265 |
| 7 | 275 |
| 8 | 284 |
| 9 | 293 |
| 10 | 300 |
| 11 | 307 |
| 12 | 314 |
| 13 | 321 |
| 14 | 327 |
| 15 | 333 |
| 16 | 338 |
| 17 | 344 |
| 18 | 349 |
| 19 | 355 |
| 20 | 360 |
| 21 | 365 |
| 22 | 370 |
| 23 | 375 |
| 24 | 380 |
| 25 | 385 |
| 26 | 390 |
| 27 | 395 |
| 28 | 400 |
| 29 | 405 |
| 30 | 411 |
| 31 | 416 |
| 32 | 421 |
| 33 | 427 |
| 34 | 433 |
| 35 | 439 |
| 36 | 445 |
| 37 | 451 |
| 38 | 458 |
| 39 | 465 |
| 40 | 473 |
| 41 | 481 |
| 42 | 490 |
| 43 | 499 |
| 44 | 510 |
| 45 | 523 |
| 46 | 538 |
| 47 | 557 |
| 48 | 582 |
| 49 | 600 |
| 50 | 600 |

## A total raw score (left

column) is converted to a total scaled score (right column). The total scaled score may range from 0 to 600.

A scaled score of 400 or more means the student passed the SOL test, while a scaled score of 399 or less means the student did not pass the test. A scaled score of 500 or more indicates the student passed the SOL test at an advanced level.

